



University of Würzburg  
Dept. of Distributed Systems  
Prof. Dr. P. Tran-Gia

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## *Delay Analysis of DHT-based Peer-to-Peer Networks*

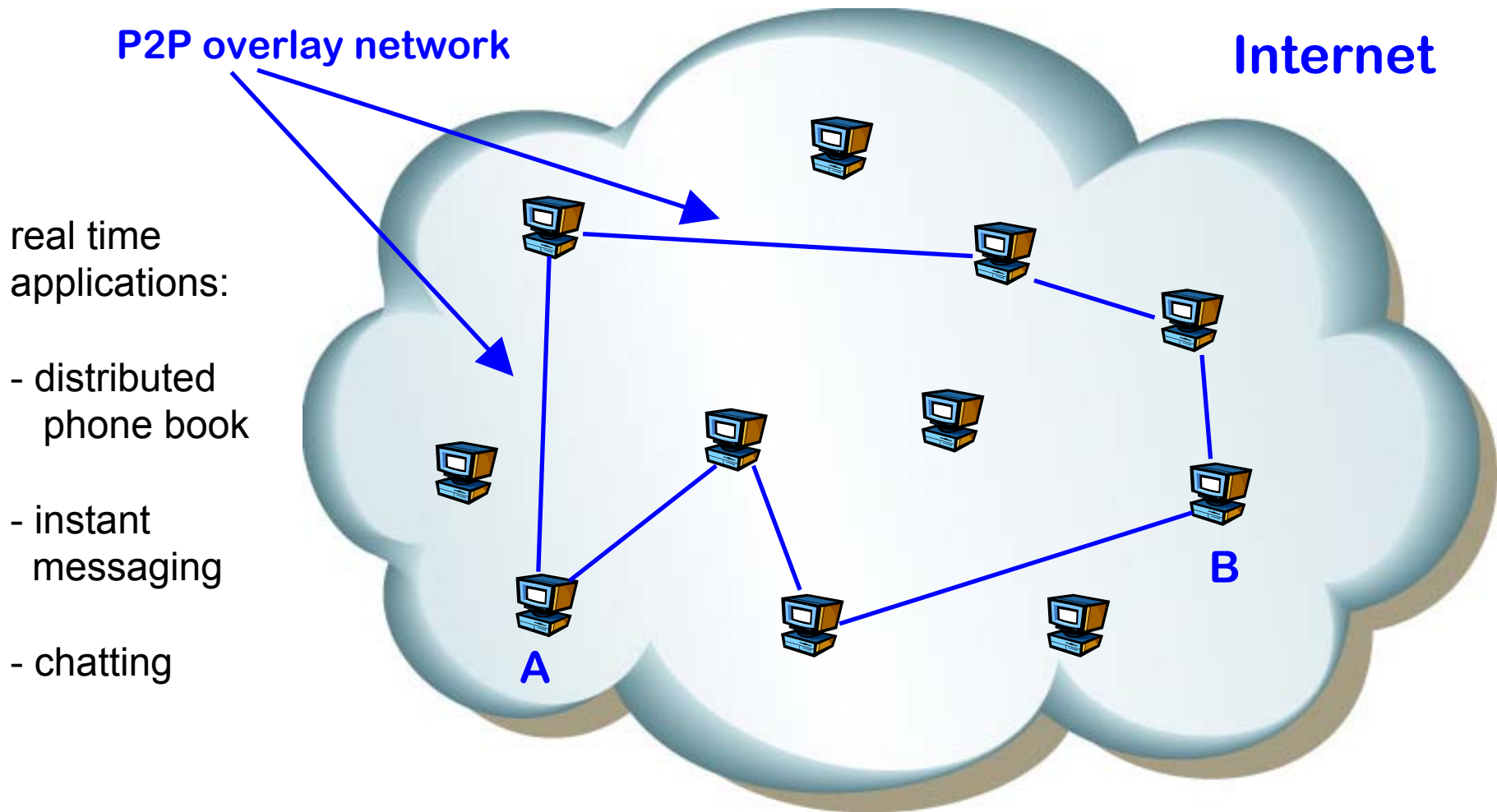
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# How to calculate the duration of a search?



# Outline

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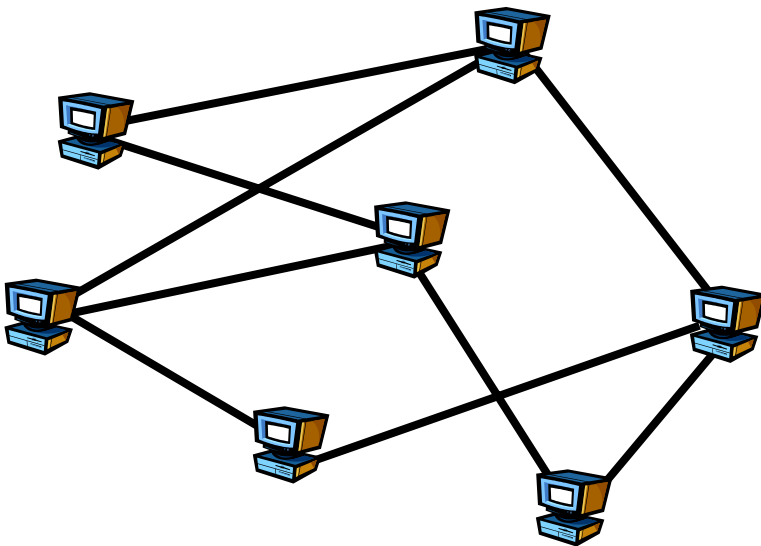
- ▷ Introduction to P2P networks
- ▷ Chord basics
  - How is a Chord ring organized?
  - How does a search in a Chord ring work?
- ▷ Analysis of the duration of a search in a Chord-based P2P-system
  - Required assumptions
  - Model of the search
- ▷ Results
  - Effects of the network variation on the search duration
  - Study of the scalability
- ▷ Conclusion



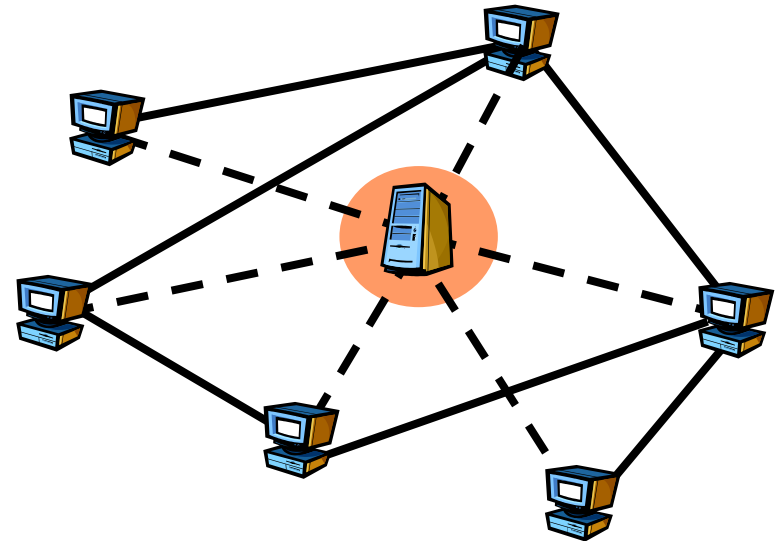
# Introduction

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- ▷ P2P-systems are mainly used to **store** and **retrieve** data



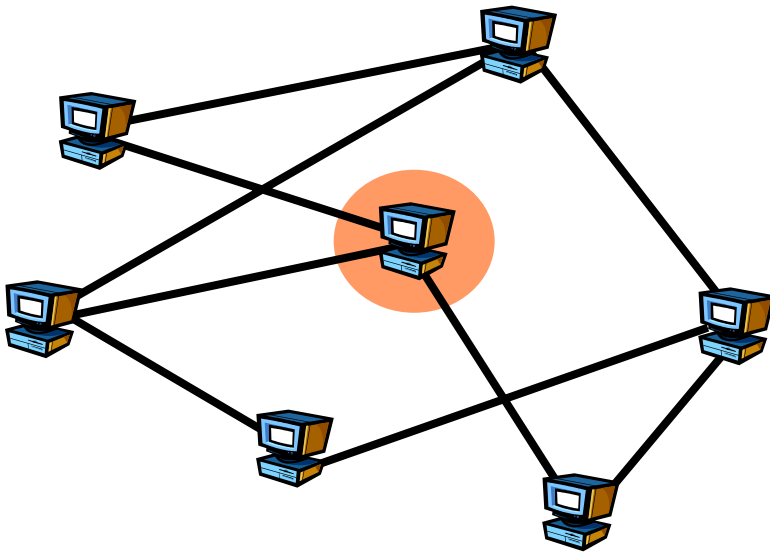
broadcasting mechanisms  
(Gnutella)



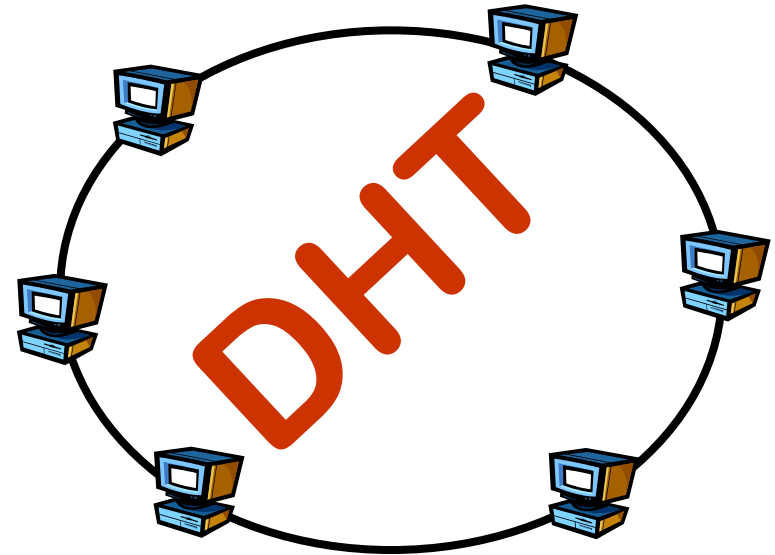
index server  
(edonkey, emule)

# Introduction

- ▷ P2P-Systems are mainly used to **store** and **retrieve** data



super peers  
(Kazaa)



structured overlay  
(Chord, Kademia)

- ▷ Little is known about the influence of the variation of the network delay on the time needed to complete a search

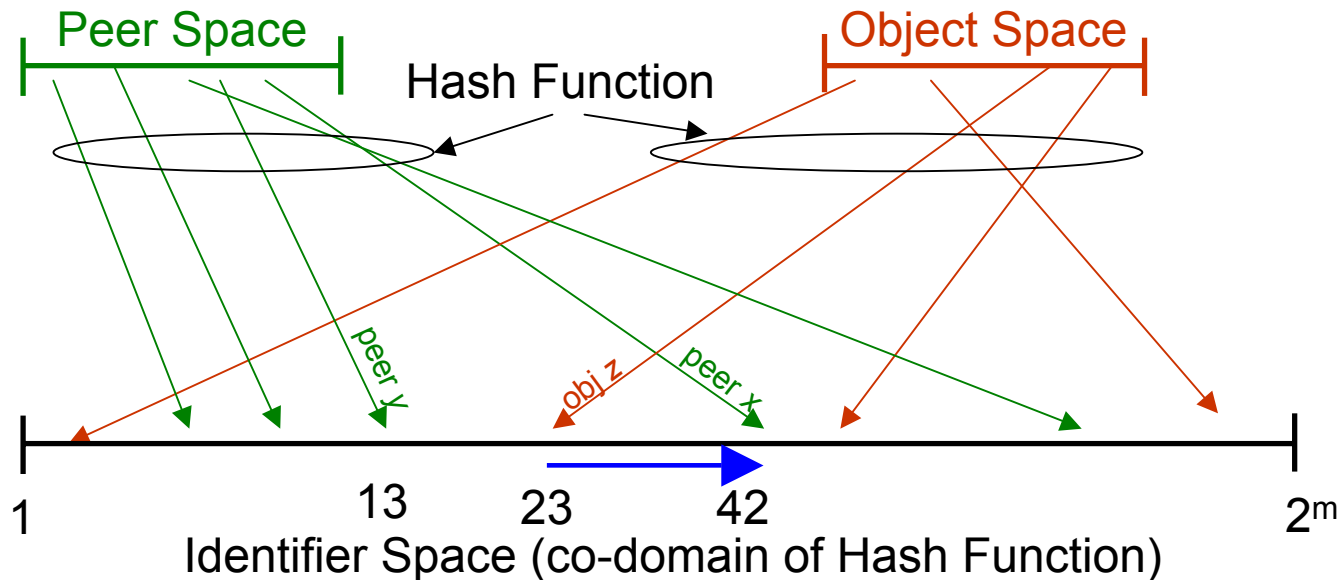
# How does a DHT work?

132.187.106.10

trangia.xml

193.136.221.1

binzenhoefer.xml

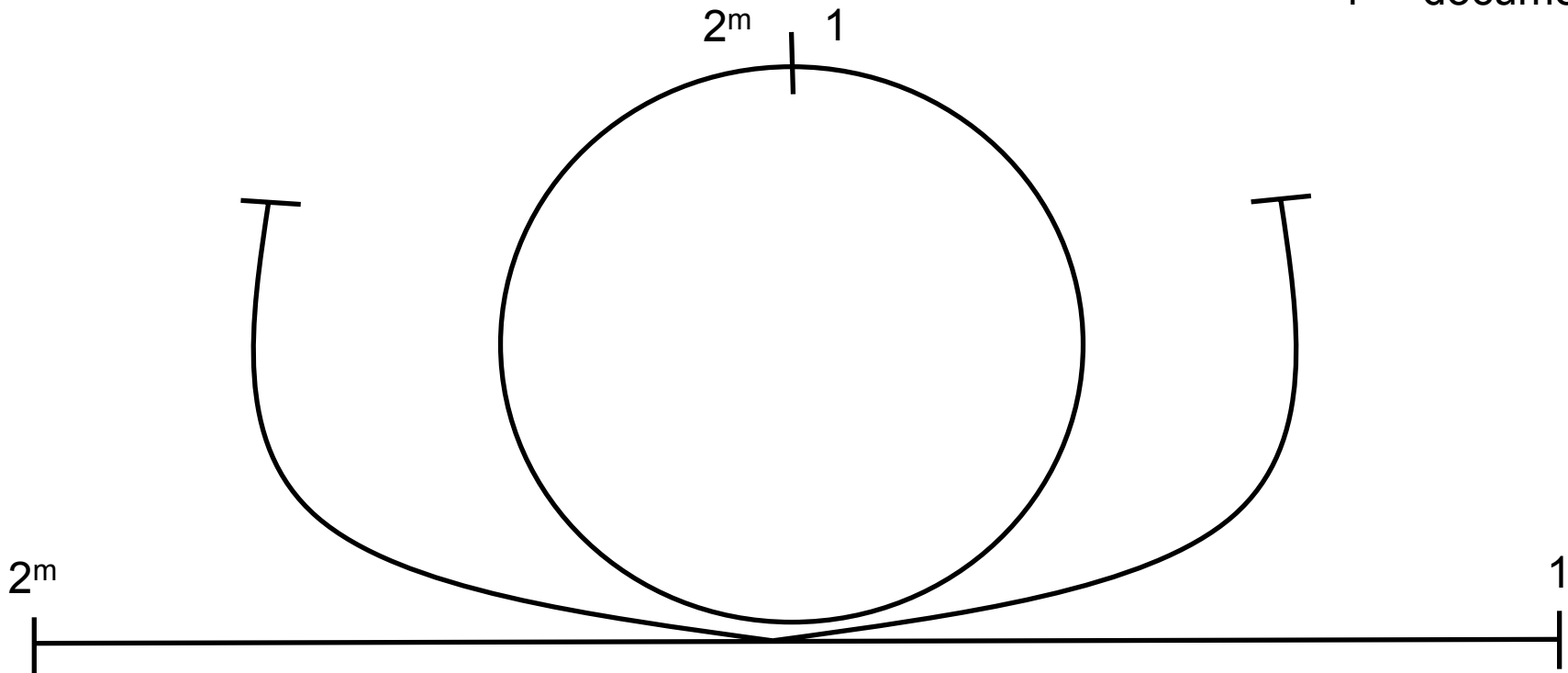


Each object is stored at the first peer succeeding the objects hash value



# Chord Example

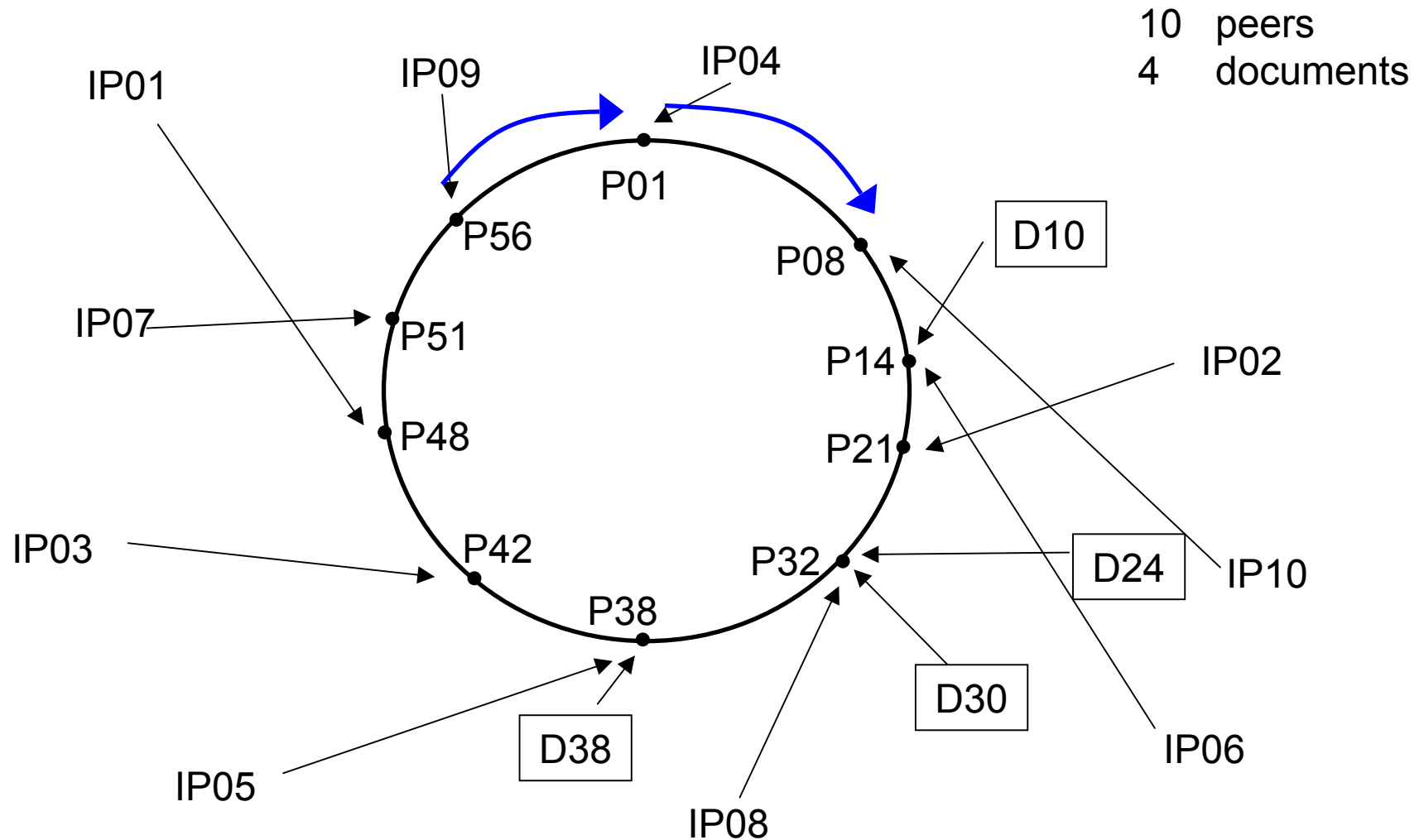
10 peers  
4 documents



- ▷ The **identifier space** is transformed into a **circle** to cope with its edges



# Chord Example





# Assumptions

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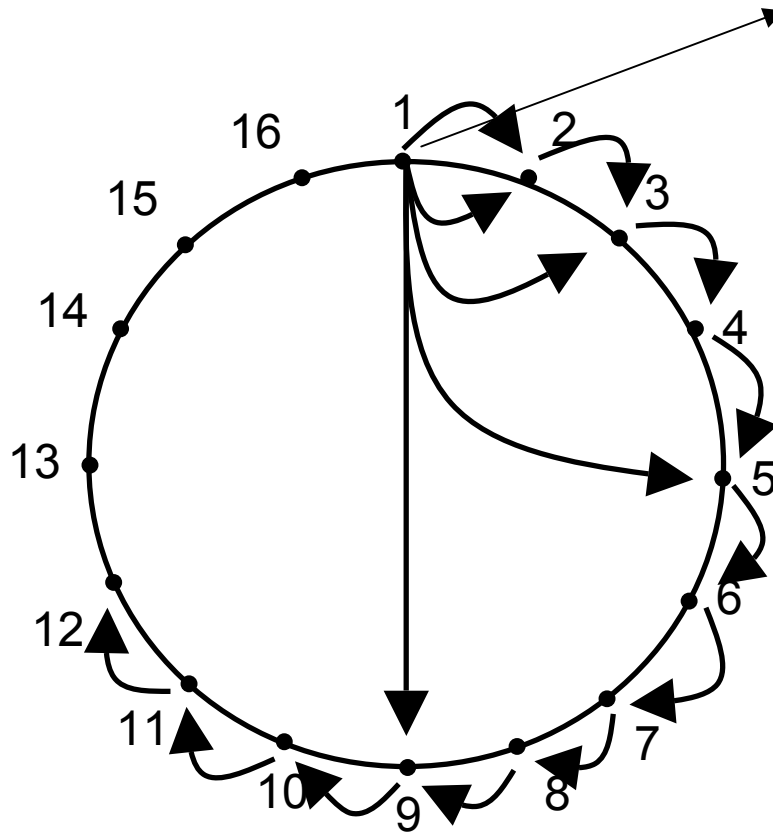
- ▷ Stable Chord ring (no changes in the overlay structure)
- ▷ All peers and documents uniformly allocated in the identifier space
- ▷ Each document looked up with the same probability
- ⇒ Each peer will be responsible for the same number of documents and will therefore answer the same number of queries.



# Chord: Fingertable

A peer with ID  $id_p$   
has its  $i$ -th finger at:

$$id_p + 2^{(i-1)}$$



The peer with  $id_p=1$  has  
its fingers at:

$$2 = 1 + 1$$

$$3 = 1 + 2$$

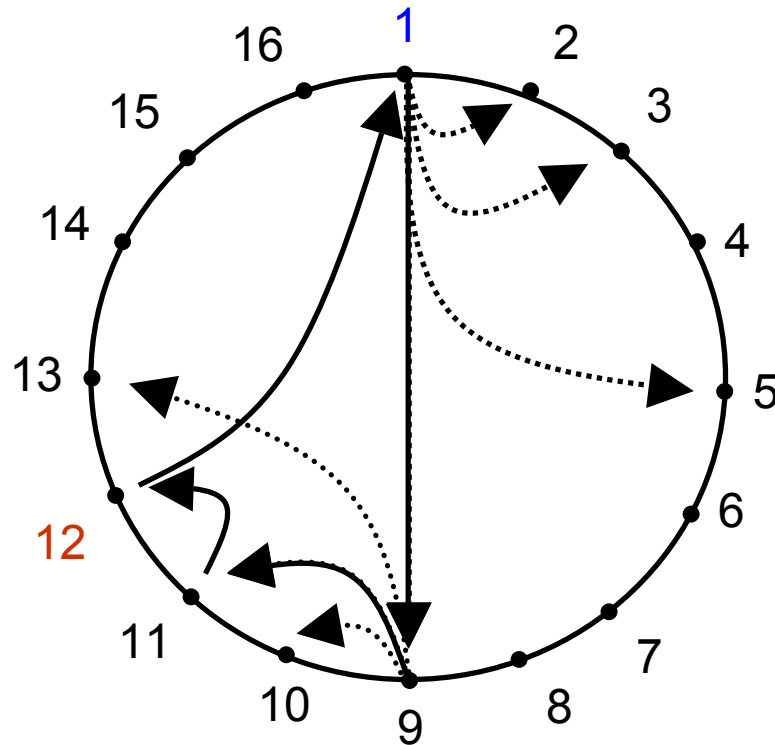
$$5 = 1 + 4 \text{ and}$$

$$9 = 1 + 8$$



# Chord: Search

peer 1 is looking up peer 12



A search is always forwarded to the closest peer



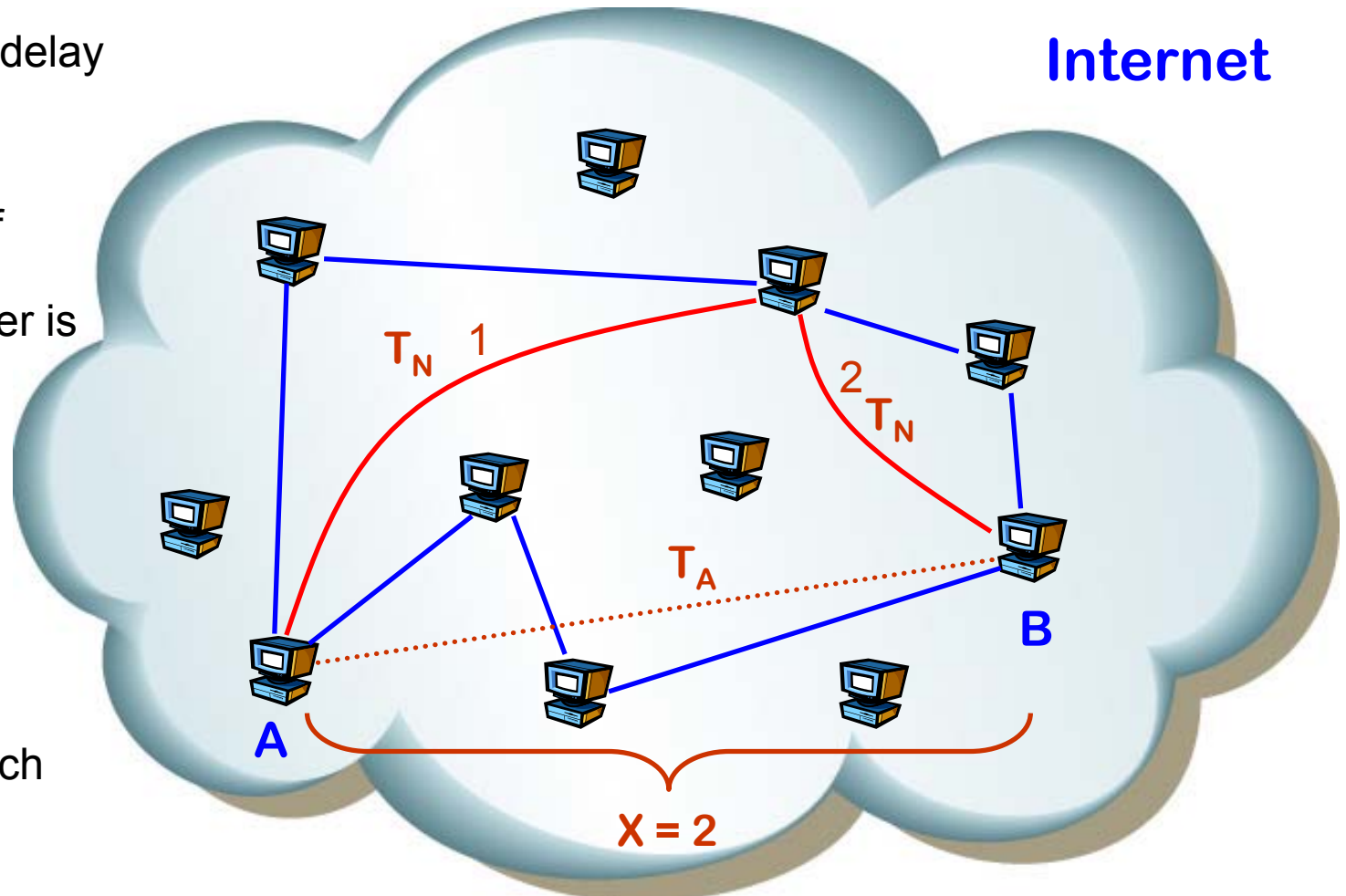
# Definitions

▷  $T_N$ : one hop delay

▷  $X$ : number of hops until searched peer is found

▷  $T_A$ : delay of the answer

▷  $T$ : total search duration



⇒ needed later to calculate quantiles



# Distance Distribution: special case

Assume Chord Size:  $n = 2^k$

Number of peers that are  $i$  hops away:

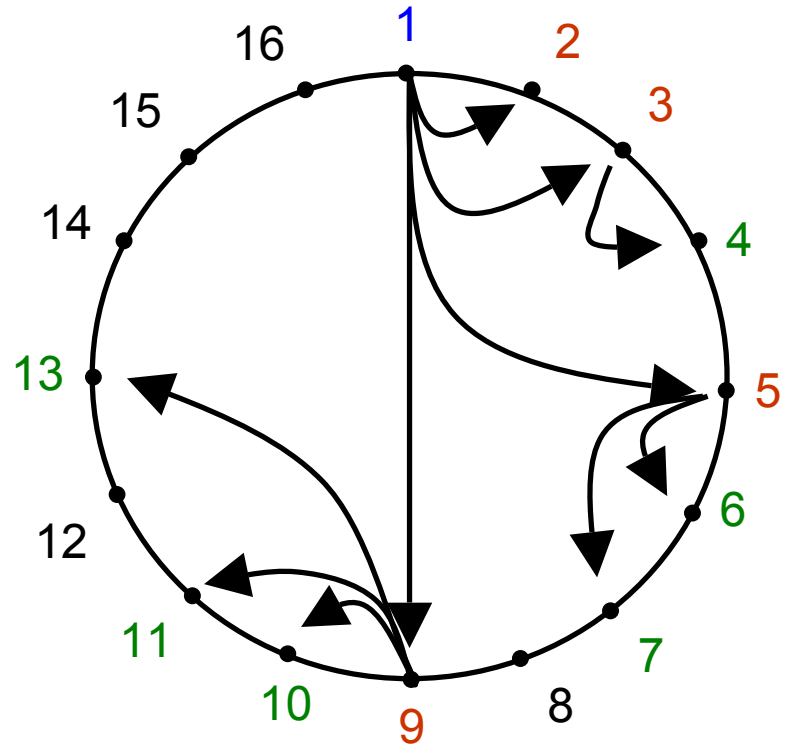
**0 hops:** 1 peer (only **peer 1** itself)

**1 hop :** 4 peers (**all Fingers**)

**2 hops:** 6 peers (**4, 6, 7, 10, 11, 13**)

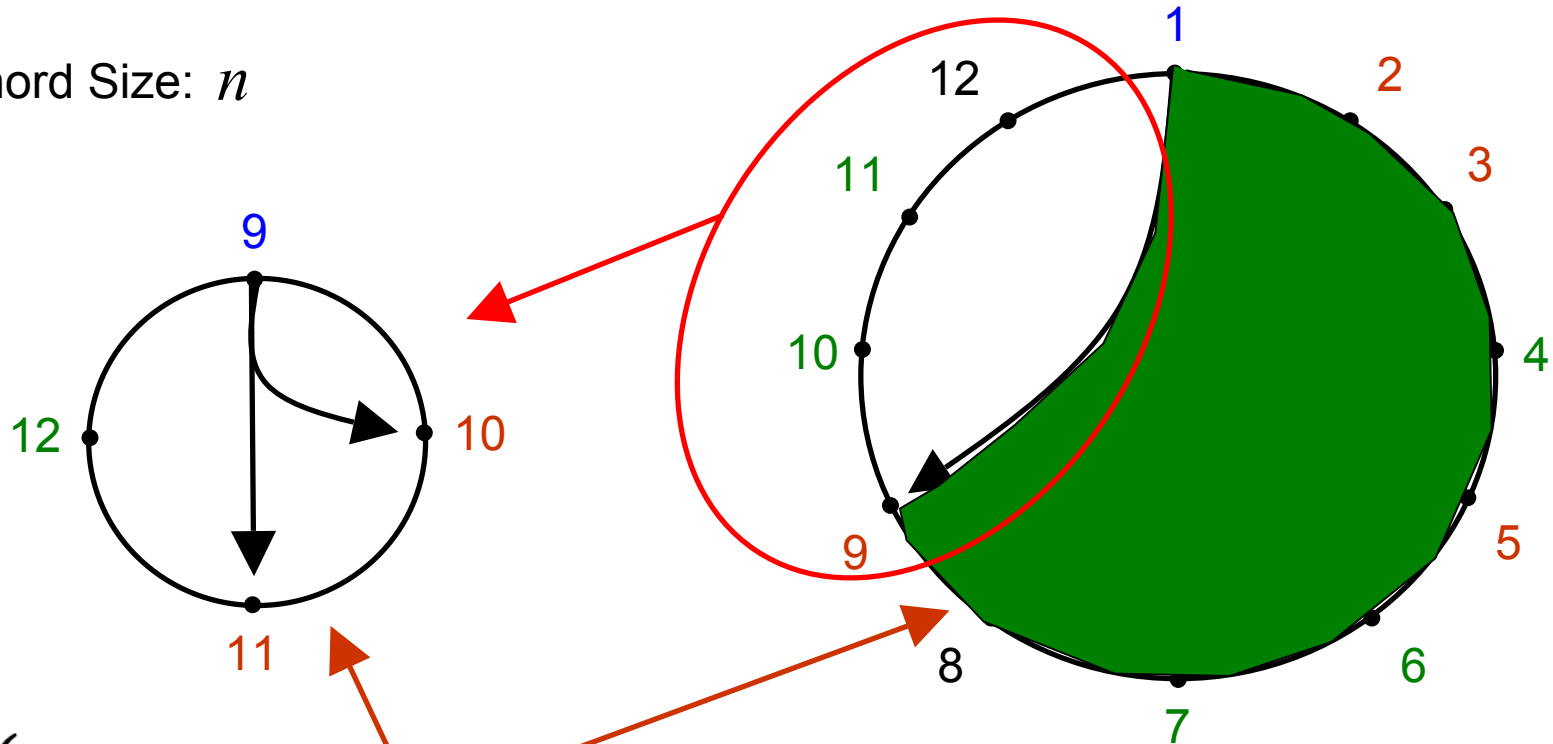
Probability, that the searched peer is  $i$  hops away

$$p_i = P(X = i) = \frac{\binom{k}{i}}{2^k}$$



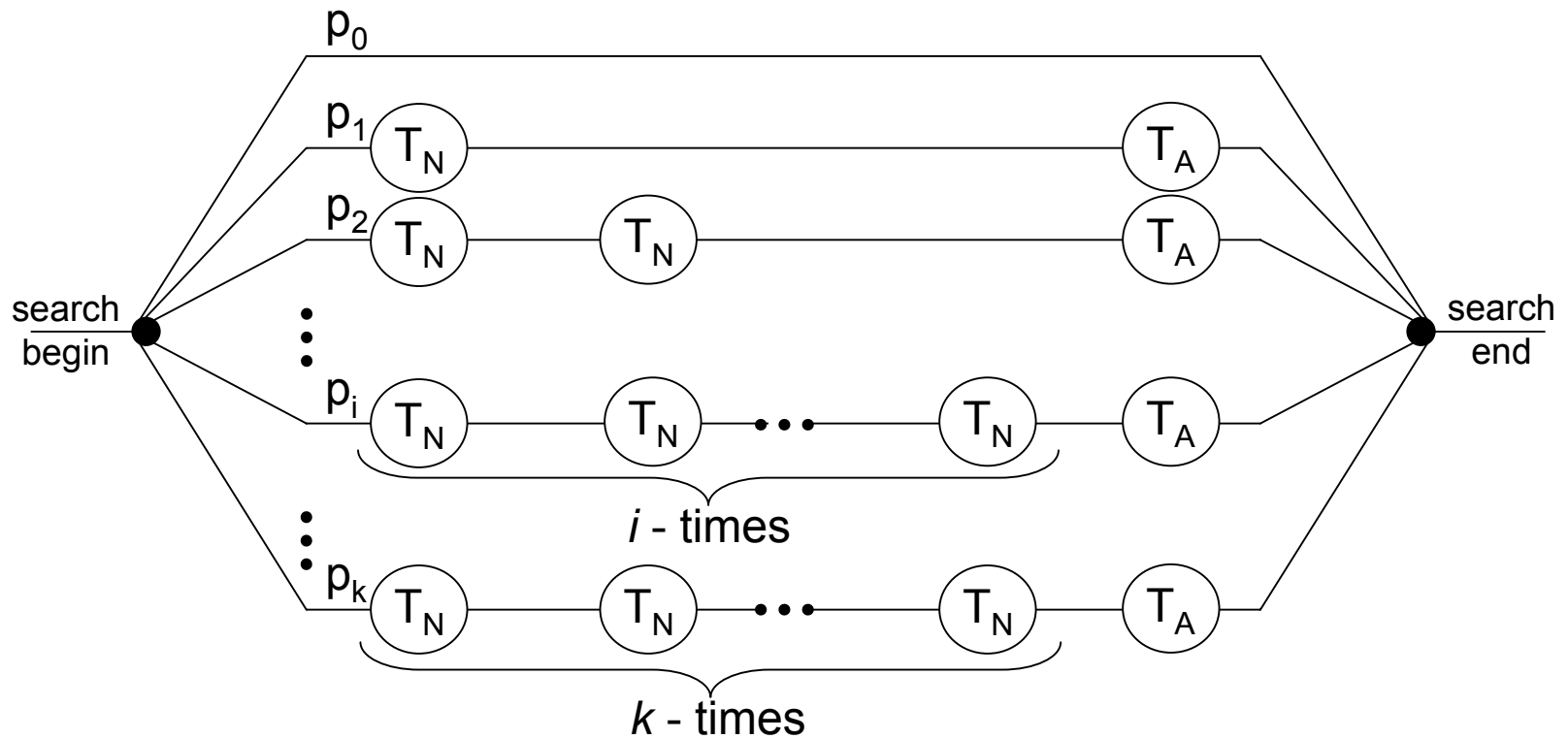
# Distance Distribution: arbitrary case

Assume Chord Size:  $n$



$$f_n(i) = \begin{cases} \binom{k}{i}, & \text{if } n = 2^k \\ \binom{k-1}{i} + f_{n-2^{k-1}}(i-1), & \text{if } 2^{k-1} < n < 2^k \end{cases}$$

# Phase Diagram of a Chord Search



# Results: Mean search delay

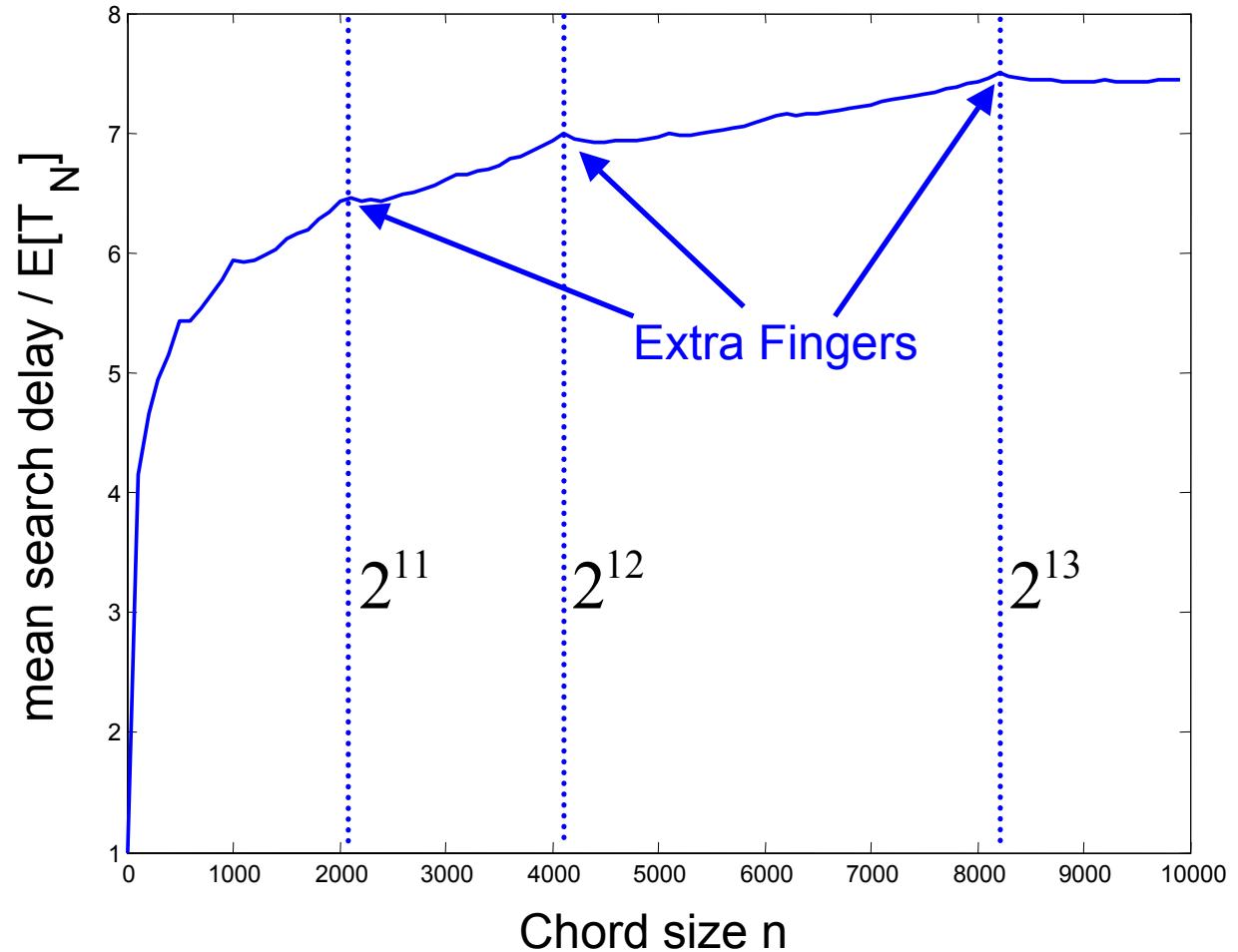
$$T_N = T_A$$

$T_N$ : negative-binomially distributed

Two moments of the network delay:

$$c_{T_N} = 1$$

$$E[T_N] = 50 \text{ ms}$$

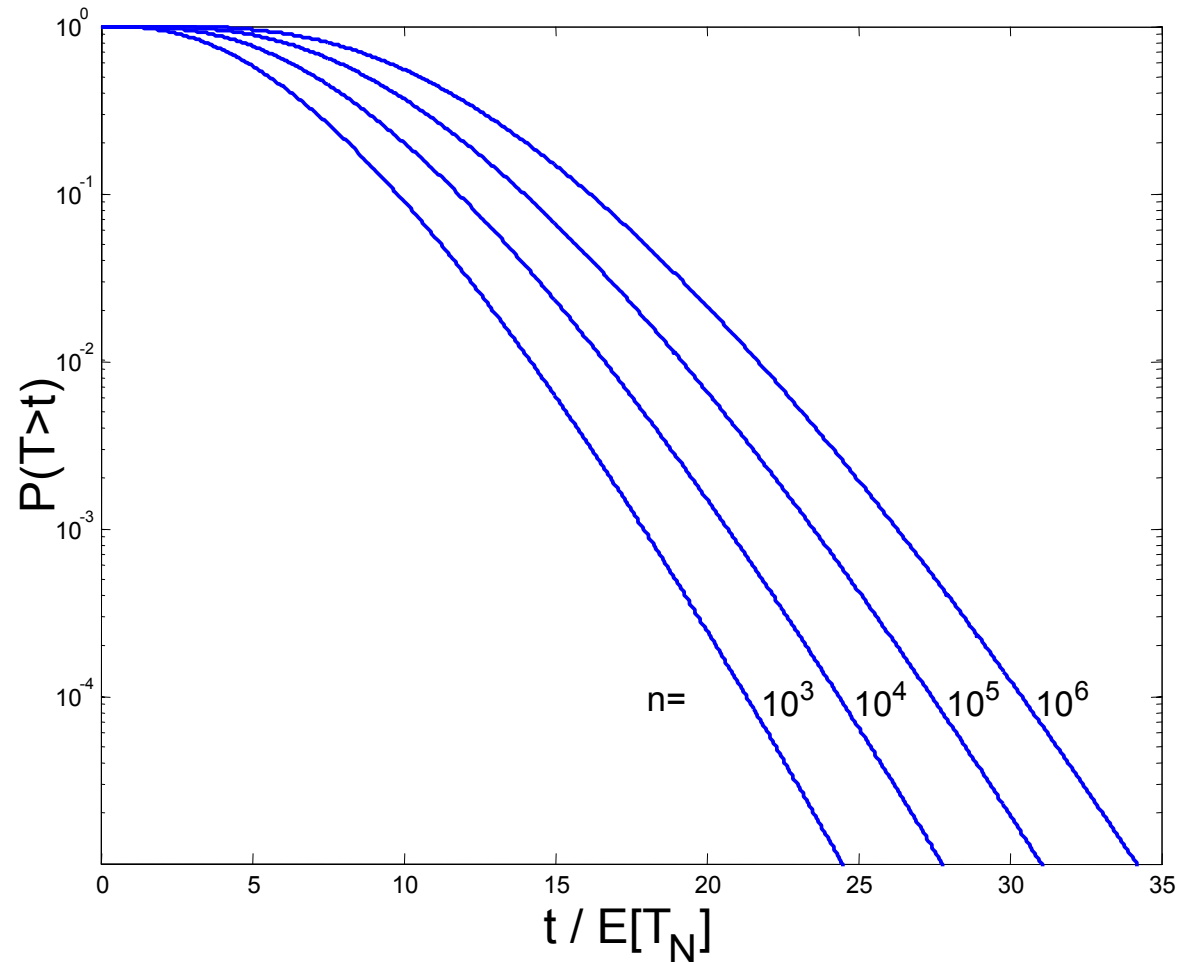




# Results: Proof of scalability

$$E[T_N] = 50 \text{ ms}$$

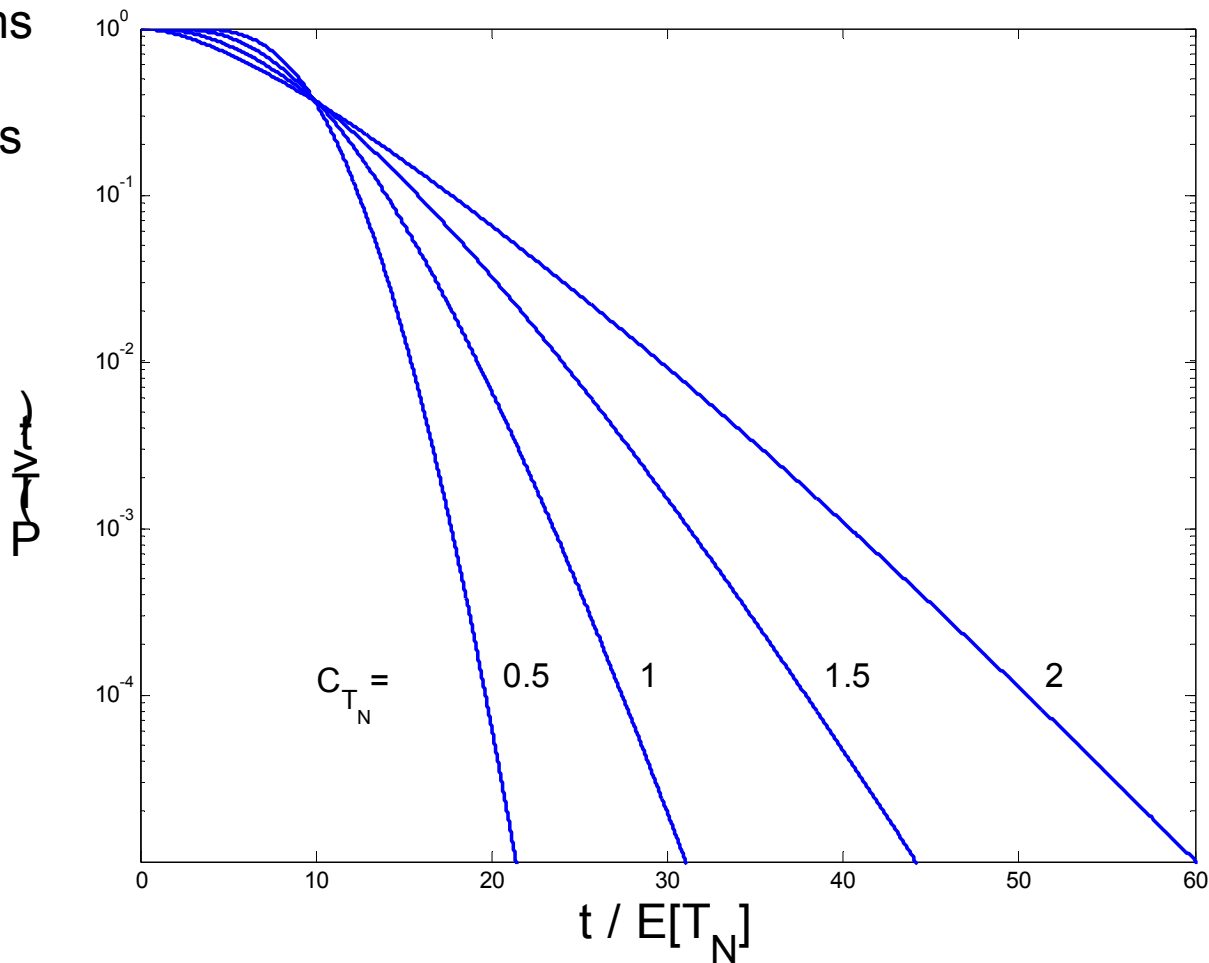
$$c_{T_N} = 1$$



# Results: Distribution Function

$E[T_N] = 50$  ms

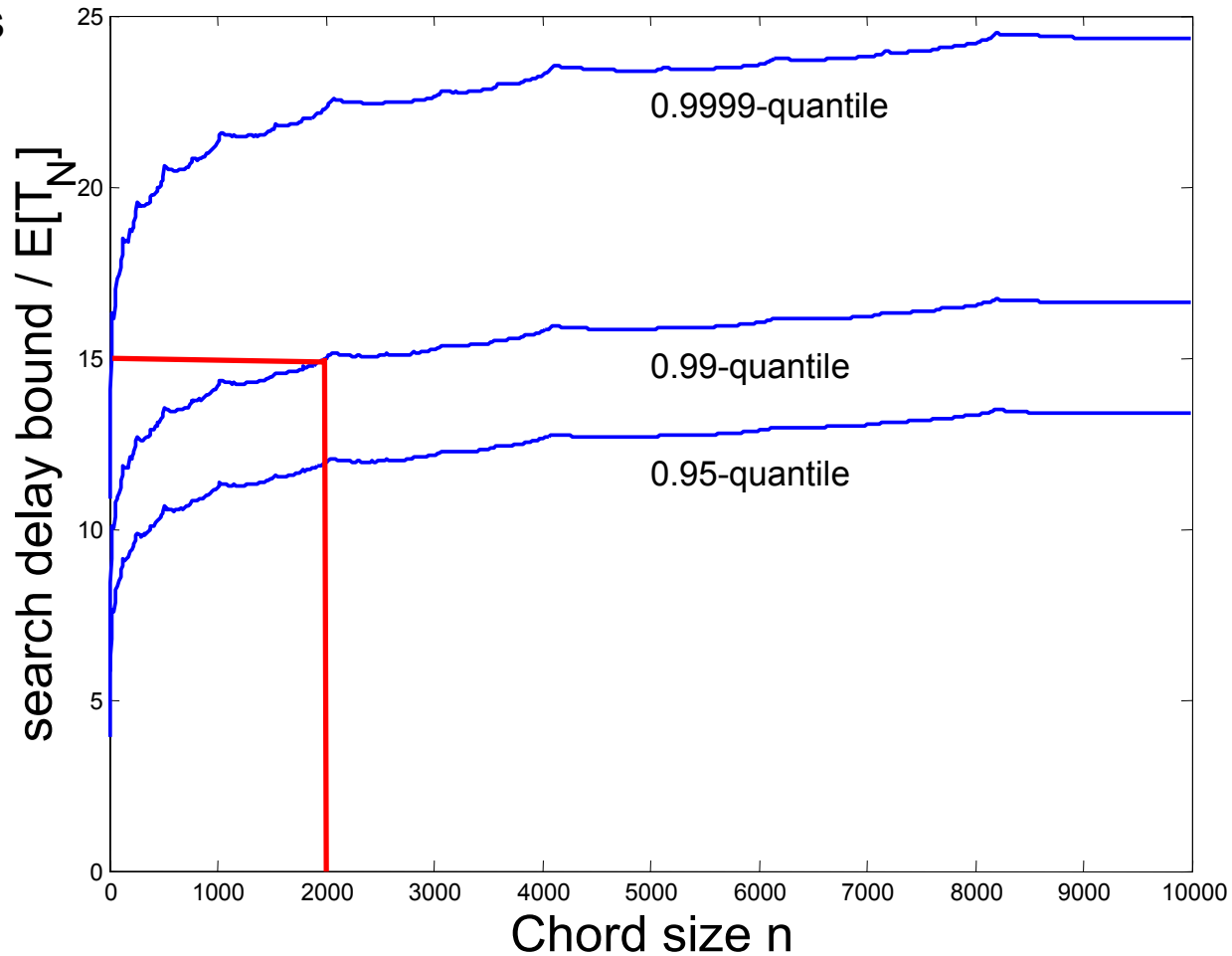
$n = 10^5$  peers



# Results: Quantiles of the search delay

$$E[T_N] = 50 \text{ ms}$$

$$c_{T_N} = 1$$



# Conclusion

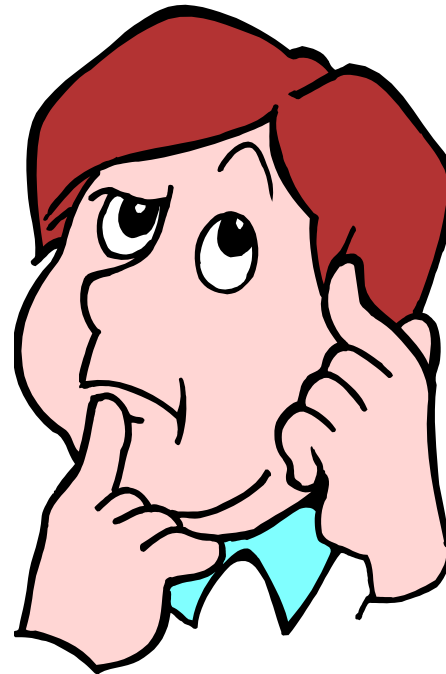
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- ▷ Search in stable Chord rings does indeed scale
- ▷ Entire distribution of the search duration can be calculated
- ▷ Quantiles of the search delay can be used for system dimensioning purposes
- ▷ Results used in a business case project regarding a distributed directory
- ▷ Extension to Chord enhancements like proximity neighbor selection possible



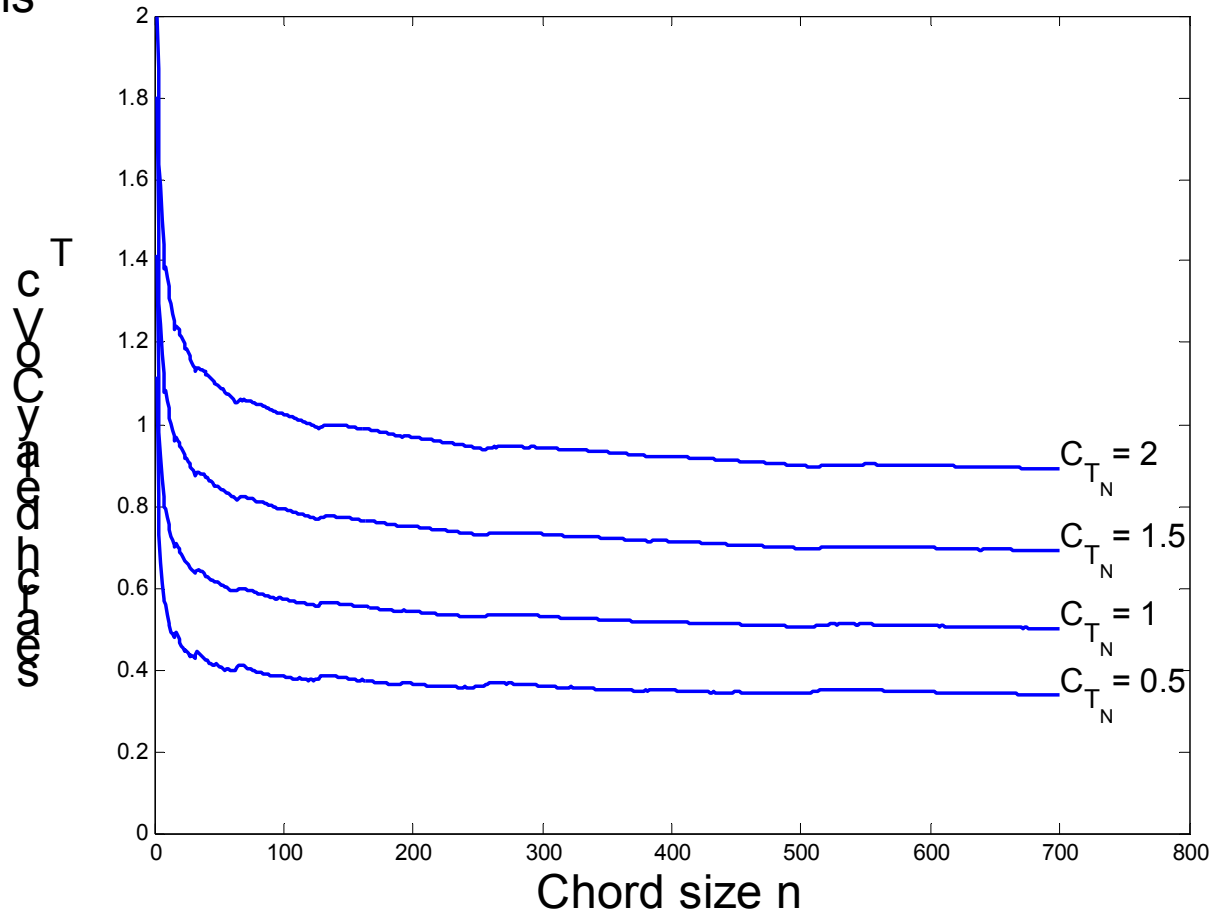
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# Q&A



# Results: CoV of the search delay

$E[T_N] = 50$  ms



# Results: CoV of the search delay

$E[T_N] = 50$  ms

